Dust growth and dust trapping in protoplanetary disks with the ngVLA

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Abstract: ALMA has revolutionized our view of protoplanetary disks, revealing structures such as gaps, rings and asymmetries that indicate dust trapping as an important mechanism in the planet formation process. However, the high resolution images have also shown that the optically thin assumption for millimeter continuum emission may not be valid and the low values of the spectral index may be related to optical depth rather than dust growth. Longer wavelength observations are essential to properly disentangle these effects. The high sensitivity and spatial resolution of the next-generation Very Large Array (ngVLA) will open up the possibilities to spatially resolve disk continuum emission at centimeter wavelengths and beyond, which allows the study of dust growth in disks in the optically thin regime and further constrain models of planet formation.
1 Introduction

The planet formation process remains one of the major puzzles in modern-day astronomy. Planets are known to form in protoplanetary disks of gas and dust around young stars (Williams & Cieza, 2011). Planet formation is hindered by a number of growth barriers, according to dust evolution theory, while observational evidence indicates that somehow these barriers must have been overcome. The core accretion process, where the accretion of dust particles and planetesimals results in solid cores of \( \sim \) Earth mass, followed by runaway gas accretion, is a promising mechanism to form the range of planets that are seen in both our Solar System and beyond (e.g. Winn & Fabrycky, 2015). However, the core accretion process requires the growth of planetesimals from submicron-sized dust grains that are seen in the interstellar medium (ISM). These first steps in dust growth in protoplanetary disks, where the dust evolution is governed by the drag forces between dust and gas, are a crucial part in the planet formation process.

In the last two decades, clear evidence has been found for dust grain evolution in disks beyond the grain sizes in the interstellar medium, through (interferometric) millimeter observations of disks (e.g. Beckwith & Sargent, 1991; Testi et al., 2003; Andrews & Williams, 2005; Natta et al., 2007; Isella et al., 2009; Ricci et al., 2010), indicating the presence of millimeter and even centimeter-sized particles in the outer regions of protoplanetary disks through multi-wavelength continuum observations and measurements of the spectral index \( \alpha_{\text{mm}} \) (mm flux \( F_{\nu} \sim \nu^{\alpha_{\text{mm}}} \)). The value of \( \alpha_{\text{mm}} \) can provide information on the particle size in protoplanetary disks (see Testi et al., 2014, and references therein). For (sub)micrometer-sized dust, such as found in the ISM (interstellar medium), \( \alpha_{\text{mm}} \) is typically 3.5–4.0, but when dust grows to mm sizes, \( \alpha_{\text{mm}} \) is expected to decrease to 2–3 (Draine, 2006; Ricci et al., 2010). When the dust emission is optically thin and in the Rayleigh-Jeans regime, the observable \( \alpha_{\text{mm}} \) can be related to the dust opacity index \( \beta = \alpha - 2 \), with \( \beta < 1 \) for mm grains and larger (Natta et al., 2004). Furthermore, \( \beta \) is related to the dust opacity of a certain dust grain size population \( n(a) \) as \( \kappa_{\nu} \propto \nu^{\beta} \), where \( \beta \) is mostly sensitive to the maximum grain size \( a_{\text{max}} \) (Draine, 2006).

In early work, grain growth in protoplanetary disks was primarily based on unresolved or marginally resolved mm data in surveys of star forming regions, showing \( \alpha_{\text{mm}} \) values well below the ISM value of 3.5–4.0, indicating mm-sized particles in the outer disk. For a long time, it remained unclear how these particles could be present, due to the so-called radial drift problem: the rapid inward drift of dust particles in a disk when grown to mm sizes (Whipple, 1972; Weidenschilling, 1977). For a disk with a smooth radial density profile, both the gas surface density and temperature decrease radially outward. The additional pressure support results in a slightly sub-Keplerian orbital velocity for the gas. In contrast, dust particles are not pressure supported and want to orbit at Keplerian speed, but as they are embedded in a sub-Keplerian gas disk, they are forced to orbit at lower speed which leads to a removal of angular momentum from the particles to the gas, causing the particles to spiral inward. The dust particles are thus experiencing a drag force by the gas, depending on its Stokes number \( St \), which describes the coupling of the particles to the gas and depends on the dust particle size and the local gas surface density (see e.g. Brauer et al., 2008; Birnstiel et al., 2010). For small dust particles, \( St \ll 1 \), they are strongly coupled to the gas and do not drift inwards, but radial drift becomes significant when the particle size increases and reaches its strongest value when \( St = 1 \). In practice, mm-dust particles in the outer disk can have \( St \) values close to unity and are expected to drift inwards on...
time scales as short as 100 years, hence further dust growth is hindered. An additional problem is fragmentation: while low-velocity collisions lead to particle growth, high-velocity impacts lead to destruction according to experimental and theoretical work on dust interaction (Blum & Wurm, 2000). The combination of the radial drift and fragmentation problems is also called the ‘meter-size barrier’ because a one-meter size object at 1 AU drifts efficiently inwards limiting further growth, and equivalently dust particles in the outer disk cannot grow beyond mm sizes.

A proposed solution to explain the presence of larger dust grains in disks as the start of planet formation, is a so-called dust trap, where dust particles are being ‘trapped’ in local pressure maxima in the outer disk (Whipple, 1972; Klahr & Henning, 1997; Rice et al., 2006; Brauer et al., 2008; Pinilla et al., 2012b). Such a pressure maximum or pressure bump can arise as a radial dust trap at the edges of dead zones (e.g. Varnière & Tagger, 2006), at the edges of gas gaps cleared by planets (Zhu et al., 2012; Pinilla et al., 2012a), in zonal flows (Johansen et al., 2009; Pinilla et al., 2012b) or as azimuthal dust traps in long-lived vortices (e.g. Barge & Sommeria, 1995; Klahr & Henning, 1997), which can be the result of a Rossby Wave Instability of a radial pressure bump (e.g. Lovelace et al., 1999; Wolf & Klahr, 2002; Lyra et al., 2009). Pressure maxima as a solution for dust growth were proposed theoretically, but without spatially resolved information on the dust grain size distribution this solution remained speculative.

The Atacama Large Millimeter/submillimeter Array (ALMA), which started operations in 2012, has revolutionized our view of protoplanetary disks, in particular on the existence of dust traps, starting with the discovery of the highly asymmetric mm-dust concentration in Oph IRS 48 (van der Marel et al., 2013, 2015a). Oph IRS 48 is an example of a transitional disk, a disk with a cleared inner dust cavity (e.g. Espaillat et al., 2014), a class of disks of particular interest in dust evolution predictions for keeping mm-sized dust grains in the outer disk (Pinilla et al., 2012a). Other transition disks imaged with ALMA show a range of azimuthally symmetric and asymmetric dust rings (Casassus et al., 2013; Zhang et al., 2014; Pérez et al., 2014; van der Marel et al., 2015b; Pinilla et al., 2017). The existence of radial dust traps was primarily indicated by the difference in distribution of the gas (as traced by CO isotopologues) and mm dust (e.g. Bruderer et al., 2014; Perez et al., 2015; van der Marel et al., 2016; Dong et al., 2017; Fedele et al., 2017) and the difference with the μm-sized dust grains (Garufi et al., 2013; Pinilla et al., 2015). Multi-wavelength ALMA observations between 1.3 and 0.45 mm provided a hint of radial trapping in the SR 21 and SR 24S disks through spatially resolved $\alpha(r)$ which decreased to $<3$ in the ring emission (Pinilla et al., 2014, 2017), and azimuthal changes in $\alpha_{\text{mm}}$ were seen in the asymmetries in HD 142527 (Casassus et al., 2015) and HD 135344B (Cazzoletti et al., 2018). Combining ALMA with VLA data at cm wavelengths results in further evidence for dust trapping (e.g. Marino et al., 2015), but the low spatial resolution and sensitivity limits the calculation of a spatially resolved $\alpha_{\text{mm}}(r)$ map.

Figure 1: Overview of disk structures observed with ALMA. There is clearly a large diversity of structures, including gaps, rings, asymmetries and clumps, which are all thought to be related to the dust trapping phenomenon. The ngVLA is expected to reveal similar structures in optically thin wavelengths.
Another spectacular ALMA result in this context is the imaging of disks at ultra high angular resolution of $\sim 20$ mas or a few AU at the distance of nearby star forming regions. The mind-blowing image of HL Tau (ALMA Partnership et al., 2015) of the ALMA Long Baseline Campaign has revealed that even dust disks without inner cavity may exist of ring-like structures, which a remarkable similarity to the predictions of Pinilla et al. (2012b) of local pressure maxima that are required for the explanation of mm-sized dust in the outer disk. Since then, dozens of other disks observed at high angular resolution revealed ring-like structures (e.g. Andrews et al., 2018; van der Marel et al., 2019). If the dust rings are also caused by planets, trapping is expected to occur. Multi-wavelength observations indeed reveal radial variations of $\alpha_{mm}$ along the gaps and rings in HL Tau and TW Hya (Carrasco-González et al., 2016; Tsukagoshi et al., 2016), but the evidence is still marginal with the currently available data.

On the other hand, evidence for radial drift is evident in observations. SMA observations already revealed evidence for a segregation between the dust and gas in the IM Lup disk (Panić & Hogerheijde, 2009), with the gas outer radius being twice as large as that of the dust. Multi-wavelength continuum observations show a decrease of particle grain size with radius for a number of primordial disks (Pérez et al., 2015; Tazzari et al., 2016; Tripathi et al., 2018). Clearly, in lack of one or more dust traps in the outer disk, dust particles do drift inwards to the nearest pressure maximum. On the other hand, this implies that any extended dust disk must in fact consist of one or more pressure bumps, to keep the dust particles away from the center of the disk.

2 The optical depth problem

The results described above appear very promising in explaining the presence of large dust grains in protoplanetary disks as the start of the planet formation process, but they suffer from a major problem: the spectral index $\alpha_{mm}$ can only be related to $\beta$ in a simple linear fashion for optically thin emission. The optical depth $\tau_\nu(r)$ is defined as

$$
\tau_\nu(r) = \int_{-\infty}^{\infty} \rho \kappa_\nu ds = \frac{\kappa_\nu \Sigma(r)}{\cos i}
$$

with $\Sigma(r)$ the dust surface density at radius $r$ and $i$ the inclination and the emitted flux $F_\nu$ integrated over a disk area can be computed as:

$$
F_\nu = \frac{\cos i}{d^2} \int B_\nu(T(r)) \left( 1 - e^{-\tau_\nu(r)} \right) 2\pi r dr
$$

with distance $d$, Planck function $B$ at temperature $T$, which reduces to $F_\nu \propto B_\nu(T) \propto \nu^2$ for optically thick emission and $F_\nu \propto \kappa_\nu B_\nu(T) \propto \nu^{2+\beta}$ for optically thin emission ($\tau_\nu \ll 1$). This immediately illustrates that the spectral index $\alpha_{mm}$ is 2 (and thus $\beta \sim 0$) for optically thick emission regardless of the grain size, and a low value of $\beta$ does not automatically imply large dust grains. The optical depth is generally estimated by comparing the measured brightness temperature $T_b$ ($T_b \sim I_\nu = \frac{F_\nu}{d^2}$) with the solid angle $d\Omega$ and the physical dust temperature $T_{dust}$ as calculated from a radiative transfer model. Interferometric disk observations do show lower values for $T_b$ than $T_{dust}$, indicating $\tau_\nu \sim 0.5$ or lower, but if the optically thick emission is concentrated on scales smaller than the resolution, optical depth effects cannot be ruled out as an explanation.
for the low $\beta$ values based on mm emission (Ricci et al., 2012; Tripathi et al., 2017). This is measured using the filling factor $f$, the fraction of the disk area which is optically thick. Thus, the evidence for dust growth and dust trapping based on spectral index values from mm observations may not be reliable. Furthermore, if the assumption of optically thin dust emission is no longer valid, this may have consequences for disk dust mass estimates from the integrated flux $F_\nu$:

$$M_{\text{dust}} = \frac{F_\nu d^2}{\kappa_\nu B_\nu(T)}$$  \hspace{1cm} (3)

If the dust emission is optically thick, the derived disk dust mass is only a lower limit. Even in high resolution ALMA observations, the mm disk emission often remains unresolved (e.g. in >30% of the disks in the Lupus survey which has a spatial resolution of 0.25” or 20 AU radius, Ansdell et al. (2018)), implying that the majority of disks are much smaller than previously thought, and their emission is potentially optically thick. However, even for partially resolved extended disks the integrated flux may be dominated by optically thick emission from either rings or from the inner part of the disk where the dust concentrates as a result of radial drift in absence of pressure maxima in the outer disk (Tripathi et al., 2018). The high spatial resolution of ALMA is a crucial factor here as high resolution observations have demonstrated that dust emission is concentrated in much narrower rings than previously thought.

## 3 The role of the next-generation VLA

In order to study dust growth in protoplanetary disks, spatially resolved multi-wavelength observations in the optically thin regime are crucial. The next-generation Very Large Array (ngVLA) offers high angular resolution (~10 mas) at long wavelengths (17-93 GHz or 3-18 mm) where $\tau_\nu \ll 1$. The sensitivity (~0.3$\mu$Jy/beam for 1 hour integration at 40 GHz) allows quality observations at high signal-to-noise, resulting in clear images of the structures in disks. The current VLA does not have the resolution or sensitivity to achieve this result in a reasonable amount of time. Of particular importance for dust growth studies is the spatially resolved spectral index $\beta_{cm}$ which can be calculated across optically thin wavelengths. This opens up a large range of possibilities to answer questions on the origins and mechanisms of the structures in disks observed by ALMA.

- **Azimuthal asymmetries**, though to be dust trapping vortices, have gained a large interest from the community, but a lot of questions regarding their origin remain unclear. A spatially resolved $\beta_{cm}(r, \phi)$ can help to disentangle azimuthal trapping from other proposed effects to explain dust asymmetries such as eccentricities (Ataiee et al., 2014; Ragusa et al., 2017), as eccentric disks would not show an azimuthal dependence of $\beta_{cm}$. Furthermore, the measurement of $\beta_{cm}(r, \phi)$ can constrain the trapping efficiency in the disk, and in combination with estimates of the gas surface density, lead to independent constraints on the viscosity and turbulence (Birnstiel et al., 2013; Lyra & Lin, 2013), which tends to diffuse the dust in the vortex. Quantitative estimates of the turbulence can further be used to estimate the time scales of dust trapping in a vortex and relate them to their observability. Also predictions of azimuthal dust grain size segregation (Baruteau & Zhu, 2016) can be tested with ngVLA observations at high angular resolution.
Spatially resolving the multi-ring systems such as HL Tau in multiple cm wavelengths will help to constrain their origin, which is currently completely unclear: cleared gaps by planets is a tempting explanation, but this requires (giant) planets at tens or even hundreds of AU away from the star, which are very rare in exoplanet demographics (Winn & Fabrycky, 2015; Bowler, 2016) and difficult to explain in reasonable time scales in planet formation theory (Helled et al., 2014). The edges of planet gaps are pressure maxima where dust is expected to be trapped; a measure of $\beta_{cm}(r)$ can immediately tell if the rings are consistent with dust traps. If not, other explanations for the origin of the rings will need to be considered.

The effects of radial drift can be tested with the ngVLA as well. In disks without pressure maxima in the outer disk, the larger dust particles are expected to drift inwards and form a sharp outer continuum edge (Birnstiel & Andrews, 2014). Although this effect has been demonstrated through comparison between the mm dust emission and the much more extended distribution of the gas as traced by the CO (e.g. Panić & Hogerheijde, 2009; Ansdell et al., 2018), a quantification of the drift and associated time scales remain unexplored due to the uncertainties introduced by the high optical depth in the inner part of the dust disk (e.g. Pèrez et al., 2015; Tazzari et al., 2016; Tripathi et al., 2018). Measuring $\beta_{cm}(r)$ in optically thin wavelengths will set better constraints on the grain size distribution within the disk and will help to constrain dust evolution models in providing better estimates for e.g. drift time scales and fragmentation.

Disk dust masses are generally derived from disk-integrated mm fluxes using the assumption of optically thin emission, but it is quite likely that this assumption is not valid, implying that many of the derived disk masses (usually calculated with the dust mass and a gas-to-dust ratio of 100) are lower limits. This has important consequences for our understanding of the dynamics in disks: gravitational instability (Boss, 1997) may occur for disk masses $>10\%$ of the stellar mass, which is generally well above our current estimates of the disk mass. However, if large amounts of the mm emission is optically thick, these disk masses are severely underestimated and gravitational instabilities could be important for disk fragmentation, dynamics and giant planet formation than currently thought. Large disk surveys with the ngVLA of nearby star forming regions of only a few hours can provide us with flux measurements of hundreds of disks at a sensitivity of $\sim 0.3M_{\text{Earth}}$, similar to current ALMA disk surveys.

4 Outlook

Whereas ALMA has revolutionized our understanding of protoplanetary disks by revealing a large diversity of structures indicating concentrated dust growth, a better understanding and quantification of the dust growth processes can only be achieved with longer wavelength observations in the centimeter regime where the dust becomes optically thin, in particular through spectral index observations. Using the Square Kilometre Array (SKA) to derive dust spectral indices using even longer wavelengths ($>5$ cm) is impractical, as the dust emission becomes too faint to be detected at high spatial resolution. The ngVLA provides unprecedented possibilities to study dust growth in disks and further explore the dust trapping process.
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